A Recursion on Neighborhood Polynomials

Abstract

The neighborhood polynomial of a graph G is the generating function of the number of vertex subsets of the graph of which the vertices have a common neighbor in G. We provide an explicit formula for the neighborhood polynomial of graph G', which is obtained from G by adding a vertex to it. This formula suggests a recursion on the neighborhood polynomials based on deleting vertices.